What is claimed is:

- 1. The process for growing single crystals, wherein crystal material is melted in a crucible and a crystal nucleus is immersed in the molten crystal material and slowly pulled out, wherein the crystal formed during the pulling is kept at a temperature close to melting temperature of the output material.
- 2. The process of claim 1 wherein the formed crystal is kept at a temperature close to the melting temperature by at least one of: shielding the crystal material, pulled out of the melt and solidified, from heat-radiation and conductivity losses and at least partly offsetting heat losses by additional heating.
- 3. The process according to claim 1, wherein during the slow pulling-out of the crystal nucleus, a low temperature gradient is set between molten crystal material and the single crystal pulled out of the melt.
- 4. The process according to claim 2, wherein during the slow pulling-out of the crystal nucleus, a low temperature gradient is set between molten crystal material and the single crystal pulled out of the melt.
- 5. The process according to claim 2, wherein shielding and additional heating are arranged in such a way that an essentially constant temperature gradient is set in the pulling direction of the crystal.

- 6. The process according to claim 1, wherein the temperature gradient in the solidified crystal material is kept below a maximum value of 4°K/cm during the pulling.
- 7. The process according to claim 2, wherein the temperature gradient in the solidified crystal material is kept below a maximum value of 4°K/cm during the pulling.
- 8. The process according to claim 2, wherein after the pulling of the crystal, the maximum temperature gradient inside the crystal is set to a value below 3°K/cm and the whole crystal is cooled down evenly.
- 9. The process according to claim 1, wherein the crucible, at least while the crystal is slowly pulled out, is arranged in a tube made from electrically conductive material, which serves as a susceptor, and the tube is heated inductively.
- 10. The process according to claim 2, wherein the crucible, at least while the crystal is slowly pulled out, is arranged in a tube made from electrically conductive material, which serves as a susceptor, and the tube is heated inductively.

- 11. The process according to claim 1, wherein at least the slow pulling-out takes place under vacuum, i.e. preferably under a pressure of between 10^{-2} and 10^{-8} hectopascals.
- 12. The process according to claim 2, wherein at least the slow pulling-out takes place under vacuum.
- 13. The process of claim 12, wherein the slow pulling-out takes place at a pressure of between 10^{-2} and 10^{-8} hectopascals.
- 14. The process according to claim 1, wherein at least the slow pulling-out takes place in a growing atmosphere selected from the group consisting of argon; nitrogen; a mixture of argon and oxygen, the oxygen proportion preferably being between 0 and 2 vol.-%; a mixture of nitrogen and oxygen, the oxygen proportion preferably being between 0 and 2 vol.-%; and a mixture of argon and hydrogen, the hydrogen proportion preferably being between 0 and 10 vol.-%.
- 15. The process according to claim 2, wherein at least the slow pulling-out takes place in a growing atmosphere selected from the group consisting of argon; nitrogen; a mixture of argon and oxygen, the oxygen proportion preferably being between 0 and 2 vol.-%; a mixture of nitrogen and oxygen, the oxygen proportion preferably being between 0 and 2 vol.-%; and a mixture of argon and hydrogen, the hydrogen proportion preferably being between 0 and 10 vol.-%.

- 16. The process according to claim 1, wherein the temperature in the environment of the crucible is controlled.
- 17. The process according to claim 2, wherein the temperature in the environment of the crucible is controlled.
- 18. The process according to claim 16, wherein the temperature in the environment of the crucible is controlled by suitable choice of the inductor dimension and the susceptor geometry.
- 19. The process according to claim 1, wherein the temperature gradient along the single crystal grown is controlled or regulated between molten crystal material and the crystal nucleus.
- 20. The process according to claim 19, wherein the setting of the temperature gradient takes place by means of the inductor dimension and the susceptor geometry.
- 21. The process according to claim 9, wherein susceptor material is selected depending on crucible material and growing atmosphere.
- 22. The process according to claim 1, wherein a non-metal crystal nucleus is used.

- 23. The process according to claim 1, wherein a corundum crystal nucleus (Al₂O₃) is used.
- 24. The process according to claim 2, wherein a corundum crystal nucleus (Al₂O₃) is used.
- 25. The process according to claim 1, wherein the crystal nucleus is immersed in the crystal material and slowly pulled out in approximately the direction of the crystallographic c-axis with a deviation of less than $\pm 15^{\circ}$.
- 26. A device for growing single crystals having a crucible to receive molten crystal material, a heating device for heating the crucible and the crystal material and a device for pulling the crystal out of the melt using an immersed crystal nucleus wherein at least one of a shield and heating element is provided surrounding the crystal during the pulling which prevents rapid cooling of the solidified crystal material in comparison with the melt and a large temperature gradient within solidified crystal material.
- 27. A device according to claim 26, wherein the heating device consists of a susceptor tube made from electrically conductive material inside of which the crucible is arranged, and an inductor which heats the tube inductively.

- 28. A device according to claim 27, wherein the tube consists of graphite, tungsten, molybdenum, iridium, rhenium, tantalum, osmium, or an allow of the abovementioned elements.
- 29. A device according to claim 27, wherein susceptor length is adjustable.
- 30. A device according to claim 27, wherein the position of the inductor is adjustable.
- 31. A device according to claim 26, wherein the crucible consists of iridium, molybdenum, tungsten, rhenium, tantalum, osmium, or an alloy of the abovementioned elements.
- 32. A device according to claim 27, wherein the crucible consists of iridium, molybdenum, tungsten, rhenium, tantalum, osmium, or an alloy of the abovementioned elements.